## CS 70Discrete Mathematics and Probability TheoryFall 2019Alistair Sinclair and Yun S. SongDIS 7

## 1 Farmer's Market

Suppose you want k items from the farmer's market. Count how many ways you can do this, assuming:

- (a) There are pumpkins and apples at the market.
- (b) There are pumpkins, apples, oranges, and pears at the market
- (c) There are n kinds of fruits at the market, and you want to end up with at least two different types of fruit.

## 2 Counting Practice

- (a) If you shuffle two (identical) decks of cards together, you get a stack of 104 cards, where each different card type is included twice. How many different ways are there to order this stack of cards?
- (b) How many different anagrams of GHOST are there if: (1) H is the right neighbor of G; (2) G is on the left of H (and not necessarily H's neighbor)?
- (c) There are 20 socks in a drawer, none of which match. How many different ways are there to pair up these socks? (Assume that any sock can be paired with any other sock.)

## 3 Counting on Graphs

- (a) How many distinct undirected graphs are there with *n* labeled vertices? Assume that there can be at most one edge between any two vertices, and there are no edges from a vertex to itself. The graphs do not have to be connected.
- (b) How many ways are there to color a bracelet with *n* beads using *n* colors, such that each bead has a different color? Note: two colorings are considered the same if one of them can be obtained by rotating the other.
- (c) How many ways are there to color the faces of a cube using exactly 6 colors, such that each face has a different color? Note: two colorings are considered the same if one of them can be obtained by rotating the other.